
Aphros documentation

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1 Introduction

Aphros is a finite volume solver for incompressible multiphase flows with surface tension. Key features:

- implementation in C++14
- abstractions for mesh elements (cells, faces and nodes), range-based loops over them and the corresponding data fields (cell-, face- and node-based fields)
- convenient and fast development (no need to write 3D loops) using only standard features of the language (without code generators or domain-specific languages)
- scalability to thousands of compute nodes using MPI/OpenMP thanks to the Cubism library for distributed computing on structured grids
- coroutines to enable encapsulation in the block-wise processing framework
- individual solvers can be used separately as regular classes or functions
- fluid solver based on SIMPLE or Bell-Colella-Glaz methods
- conservative split advection solver based on PLIC
- method of particles for curvature estimation that outperforms standard techniques at low resolutions which is well-suited for simulation with many small bubbles and drops
- multilayer volume-of-fluid scheme for coalescence prevention which has the computational cost that does not depend on the number of bubbles in the simulation and therefore can describe processes such as generation of foam

The source code is available on [GitHub](#).

2 Communication

The grid is decomposed into subdomains, one for each MPI rank. Each subdomain is further divided into cubic blocks of fixed size. The program is built following the SPMD (single program multiple data) model. Each MPI rank processes its blocks sequentially. The code is divided into *stages* which are executed in parallel on all blocks with synchronization after every stage. This implements *coroutines*. The code can issue communication requests which are collected during each stage and executed before transferring to the next stage.

The following function consists of two stages:

```

void F(Mesh& m) {
    auto sem = m.GetSem();
    struct {
        FieldCell<Scal> fc;
    }* ctx(sem);

    if (sem()) {
        fc.Reinit(m, m.GetId());
        m.Comm(&fc);
    }

    if (sem()) {
        fc.Reinit(m, 0);
    }
}

```

Mesh m provides functionality for parallel communication. Pointer ctx will be initialized to point at an instance of the user-defined *struct* persistent across stages of one call of the function. The instance is created before the execution of the first stage and destroyed after the last stage.

Communication requests include:

```
void Comm(std::unique_ptr<CommRequest>&& r)
```

```
void Reduce(std::unique_ptr<Op>&& o)
```

```
void GatherToLead(std::vector<T>* buf)
```

```
void Dump(const FieldCell<Scal>* field, std::string name)
```

3 Convection-diffusion equation

Abstract class `ConvDiffVect` describes the interface of a solver for the vector convection-diffusion equation

$$\rho \left(\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{u} \right) = \nabla \cdot (\mu \nabla \mathbf{u}) + \mathbf{f}$$

in the discrete form

$$\rho_c \left(\frac{\delta \mathbf{u}_c}{\delta t} + \frac{1}{V_c} \sum_{f \in c} v_f \mathbf{u}_f S_f^c \right) = \frac{1}{V_c} \sum_{f \in c} \mu_f \frac{\delta \mathbf{u}_f}{\delta n} S_f^c + \mathbf{f}_c \quad (3.1)$$

where c is a cell index, ϕ_c is a cell-average, $f \in c$ are neighbour faces of cell c , ϕ_f is a face-average, S_f^c is the signed face area (positive if \mathbf{n}_f is an outer normal to c) and V_c is the cell volume.

The constructor takes pointers to fields of density ρ , viscosity μ , force \mathbf{f} and volume flux $\mathbf{v} \cdot \mathbf{S}_f$:

```

// par: parameters
// fcr: density
// ffd: diffusion coefficient
// fcs: source
// ffv: volume flux
ConvDiffVect (
    double time, double dt, M& m_, const EB& eb_, Par par_,
    const FieldCell<Scal>* fcr, const FieldFaceb<Scal>* ffd,
    const FieldCell<Vect>* fcs, const FieldFaceb<Scal>* ffv)

```

After an implementation is constructed, the solution is advanced by calling `MakeIteration()` and the current velocity field is returned by

```
virtual const FieldCell<Vect>& GetVelocity(Step) const
```

The interface also exposes functions

```
virtual void Assemble(
    const FieldCell<Vect>& fcw, const FieldFaceb<Scal>& ffv)
```

```
// linear system returned by GetDiag() and GetConst()
virtual void Assemble(
    const FieldCell<Vect>& fcw, const FieldFaceb<Scal>& ffv)
```

```
// linear system returned by GetDiag() and GetConst()
virtual void Assemble(
    const FieldCell<Vect>& fcw, const FieldFaceb<Scal>& ffv)
```

to assemble the linear system for a given velocity field `fcw` from the previous iteration and the volume flux `ffv` and access its scalar component `d`. Furthermore, the current solution can be explicitly corrected with

```
virtual void CorrectVelocity(Step, const FieldCell<Vect>&)
```

Both these features are required for the pressure correction equation.

3.1 Implicit solver

Class `ConvDiffVectImp` implements an implicit solver corresponding to the discrete equation

$$\rho_c^s \left(\frac{\delta \mathbf{u}_c^{s+1}}{\delta t} + \frac{1}{V_c} \sum_{f \in c} v_f^s \mathbf{u}_f^{s+1} S_f^c \right) = \frac{1}{V_c} \sum_{f \in c} \mu_f^s \frac{\delta \mathbf{u}_f^{s+1}}{\delta n} S_f^c + \mathbf{f}_c^s$$

which requires solving a linear system at every iteration.

In addition to the requirements of the base class, the constructor takes mappings describing the boundary conditions and the initial fields:

```
// ffv: volume flux
ConvDiffVect(
    double time, double dt, M& m_, const EB& eb_, Par par_,
    const FieldCell<Scal>* fcr, const FieldFaceb<Scal>* ffd,
    const FieldCell<Vect>* fcs, const FieldFaceb<Scal>* ffv)
```

with the initial velocity `fcvel`, face conditions `mfc`, cell conditions `mcc`, density `fcr`, viscosity `fcd`, force `fcs`, and volume flux `ffv`. Parameters of the solver are provided by

```
struct ConvDiffPar {
    Scal relax = 1.; // relaxation factor [0,1] (1 -- no relaxation)
    bool second = true; // second order in time
    ConvSc sc = ConvSc::quick; // scheme for convective flux (see convdiffi.h)
    Scal df = 1.; // deferred correction factor
    Scal th = 1e-10; // threshold for flow direction
    bool stokes = false; // Stokes flow, disable convective fluxes and time
    bool symm = false; // use symmetric solver for linear system
    bool explconv = false; // explicit convective fluxes in case Conv::imp
};
```

where `sc` defines the interpolation scheme

Table 3.1: Interpolation schemes.

<code>ConvSc::fou</code>	First Order Upwind
<code>ConvSc::cd</code>	Central Differences (midpoint)
<code>ConvSc::sou</code>	Second Order Upwind
<code>ConvSc::quick</code>	QUICK

3.2 Explicit solver

Class `ConvDiffVectExp` implements an explicit solver corresponding to the discrete equation

$$\rho_c^s \left(\frac{\delta \mathbf{u}_c^{s+1}}{\delta t} + \frac{1}{V_c} \sum_{f \in c} v_f^s \mathbf{u}_f^s S_f^c \right) = \frac{1}{V_c} \sum_{f \in c} \mu_f^s \frac{\delta \mathbf{u}_f^s}{\delta n} S_f^c + \mathbf{f}_c^s.$$

Here the solution is advanced by explicit formulas and the linear system is constructed only to implement `Assemble()` and `GetVelocityEquations()` of the base class.

4 Navier-Stokes equations

Abstract class `FluidSolver` describes the interface of a solver for the Navier-Stokes equations

$$\begin{aligned} \nabla \cdot \mathbf{u} &= S_v \\ \rho \left(\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{u} \right) &= -\nabla p + \nabla \cdot \mu (\nabla \mathbf{u} + \nabla \mathbf{u}^T) + \mathbf{f} \end{aligned}$$

where the continuity equation is discretized as

$$\sum_{f \in c} v_f S_f^c = S_v$$

and the momentum equation as (3.1), where S_v is the volume source term.

The constructor takes pointers to fields of density ρ , viscosity μ , force \mathbf{f} and volume source S_v :

```
// fcr: density
// fcd: dynamic viscosity
// fcf: force
// febp: projections of balanced force
// fcsv: volume source
// fcsm: mass source
FluidSolver(
    double t, double dt, M& m_, const FieldCell<Scal>* fcr,
    const FieldCell<Scal>* fcd, const FieldCell<Vect>* fcf,
    const FieldEmbed<Scal>* febp, const FieldCell<Scal>* fcsv,
    const FieldCell<Scal>* fcsm)
```

After an implementation is constructed, the solution is advanced by calling `MakeIteration()` and the current solution is provided by

```
virtual const FieldCell<Vect>& GetVelocity(Step) const
```

```
virtual const FieldCell<Scal>& GetPressure(Step) const
```

```
virtual const FieldEmbed<Scal>& GetVolumeFlux(Step) const
```

The volume flux satisfies the continuity equation and the cell-based velocity satisfies the momentum equation.

4.1 SIMPLE

Class `Simple` implements the solver using the SIMPLE method.

In addition to the requirements of the base class, the constructor takes mappings describing the boundary conditions and the initial fields.

```
// par: parameters
Simple(M& m, const EB& eb, const Args& args)
```

with the initial velocity `fcw`, face conditions `mfc`, cell conditions `mcc`, density `fcρ`, viscosity `fcν`, force `fcf`, projections of well-balanced force `fcbp`, volume source `fcsv` and mass source `fcsm`. Parameters of the solver are provided by

```
struct SimplePar {
    using Scal = typename Vect::Scal;
    Scal vrelax = 0.8; // velocity relaxation factor [0,1]
    Scal prelatx = 1.; // pressure relaxation factor [0,1]
    Scal rhie = 1.; // Rhie-Chow factor [0,1] (0 disable, 1 full)
    bool second = true; // second order in time
    Vect meshvel = Vect(0); // relative mesh velocity
    size_t inletflux_numid = 0; // reduction for id from 0 to numid-1
    ConvSc convsc = ConvSc::quick; // convection scheme
    Scal convdf = 1.; // deferred correction factor
    bool stokes = false;
    bool explconv = false; // explicit convection for Conv::imp
    bool convsymm = false; // symmetric solver for linear system in convdiff
    Conv conv = Conv::imp; // convection-diffusion solver
    Scal outlet_relax = 1;
    bool explviscous = true; // enable explicit viscous terms
};
```

4.2 Projection

Class `Proj` implements the solver using Chorin's projection.

In addition to the requirements of the base class, the constructor takes mappings describing the boundary conditions and the initial fields.

```
// par: parameters
Proj(M& m, const EB& eb, const Args& args)
```

with the initial velocity `fcw`, face conditions `mfc`, cell conditions `mcc`, density `fcρ`, viscosity `fcν`, force `fcf`, projections of well-balanced force `fcbp`, volume source `fcsv` and mass source `fcsm`. Parameters of the solver are provided by

```

struct ProjPar {
  using Scal = typename Vect::value_type;
  Scal vrelax = 1; // velocity relaxation factor [0,1]
  Scal prelat = 1.; // pressure relaxation factor [0,1]
  bool second = true; // second order in time
  Vect meshvel = Vect(0); // relative mesh velocity
  size_t inletflux_numid = 0; // reduction for id from 0 to numid-1
  ConvSc convsc = ConvSc::quick; // convection scheme
  Scal convdf = 1.; // deferred correction factor
  bool stokes = false; // Stokes flow
  bool convsymm = false; // symmetric solver for linear system in convdiff
  Conv conv = Conv::imp; // convection-diffusion solver
  bool bcg = true; // Bell-Colella-Glaz scheme
  Scal outlet_relax = 1;
  Scal inletpressure_factor =
    0; // correction factor on inlet with given pressure
  bool explviscous = false; // enable explicit viscous terms
  bool redistrib_adv = false; // use RedistributeCutCellsAdvection()
  // if true else RedistributeCutCells()
  size_t diffusion_iters = 1; // number of iterations in implicit diffusion
  bool diffusion_consistent_guess = false;
};

```

4.3 Boundary conditions

The boundary conditions are specified by a map from `IdxFace` to `CondFaceFluid`, instances of which can be generated with function `solver::Parse()` from a string. Value of `id` is written to field `fluidcond` in `bc.vtk` (see *Output*).

Table 4.1: Fluid boundary conditions.

class	Parse() format	description	id
NoSlipWallFixed	wall <x y z>	no-slip wall with fixed velocity	1
InletFixed	inlet <x y z>	inlet with given velocity	3
InletFlux	inletflux <x y z id>	inlet with given total flux	3
OutletAuto	outlet	outlet	4
SlipWall	slipwall	free-slip wall	2

5 Multilayer VOF

Multilayer VOF is a method for solving the advection equation that can represent multiple interfaces in the same cell. This enables simulations of foams, suspensions, and other multiphase systems where bubbles and drops that do not coalesce.

The split conservative advection scheme Weymouth and Yue [1] operates on a volume fraction field and uses the PLIC reconstruction to compute the fluxes. In three dimensions, one advection step is split into three sub-steps, or sweeps. To ensure conservation, a divergence term is added explicitly. The normals are estimated using the mixed Youngs-centered scheme.

The multilayer VOF implements the same advection scheme but operates on *multilayer fields*. A multilayer field (u, q) stores mappings between *colors* q and *values* u . The colors are real numbers, and *none* = -1 denotes an empty color. Assuming that each cell can contain at most $L=4$ values, the mappings are represented as L -tuples up to reordering. For example, the following tuples encode a field (u, q) with three values in cell $c1$ and two values in cell $c2$

```

u[c1]: {0.2, 0.4, 0.1, 0}
q[c1]: { 0, 1, 2, none}
u[c2]: {0.3, 0.7, 0, 0}
q[c2]: { 1, 2, none, none}

```

The ordering of tuples is insignificant, so simultaneous permutation of values and colors gives equivalent representations

```

u[c1]: {0.4, 0.1, 0.2, 0}
q[c1]: { 1, 2, 0, none}
u[c2]: {0.7, 0, 0.3, 0}
q[c2]: { 2, none, 1, none}

```

A conventional field can be constructed from a multilayer field by selecting values with a given color. For example, selecting the values with color $qs=2$ gives a conventional field us

```

us[c1]: 0
us[c2]: 0.7

```

The following pseudocode implements the multilayer VOF method. One advection step is split in the spatial directions and in three dimensions consists of three substeps, or sweeps.

```

void Step() {
  for (d : {0, 1, 2}) {
    {u, q} = Sweep(d, u, v, q, n, a);
    {n, a} = Plic(u);
  }
  q = Recolor(u, q);
}

```

Given the PLIC reconstruction of the interface, one sweep computes fluxes, updates the volume fractions and propagates the colors to downwind cells

```

auto Sweep(d, u, v, q, n, a) {
  // v: mixture flux
  // w: phase flux
  // qf: phase color from upwind cell
  for (f : faces) {
    for (l : layers) {
      c = AdjacentCell(f, v[f] > 0 ? 0 : 1); // upwind cell
      w(f, l) = PlicFlux(n(c, l), a(c, l), h, v, dt, d);
      qf(f, l) = q(c, l);

      cd = AdjacentCell(f, v > 0 ? 1 : 0); // downwind cell
      if (FindLayer(q, cd, q(c, l)) == kLayerNone) {
        ld = FindLayer(q, cd, kClNone);
        if (ld != kLayerNone) {
          q(cd, ld) = q(c, l);
        }
      }
    }
  }
  for (c : cells) {
    for (l : layers) {
      fm = AdjacentCell(c, 0);
      fp = AdjacentCell(c, 1);
      ds = (v[fp] - v[fm]) * dt / volume;
    }
  }
}

```

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```
wm = w(c, FindLayer(qf, fm, q(c, l)));
wp = w(c, FindLayer(qf, fp, q(c, l)));
dl = (wp - wm) * dt / vol;
u(c, l) += udiv(c, l) * ds - dl;
if (u(c, l) == 0) {
    q(c, l) = kClNone;
}
}
}
return {u, q};
}
```

Function `Plic()` builds the PLIC reconstruction in interfacial cells and returns normals n and plane constants a :

```
auto Plic() {
    for (c : cells) {
        for (l : layers) {
            uu = Stencil3(c, u, q, q(c, l));
            n(c, l) = Normal(uu);
        }
        auto navg = Avg(n, q, c);
        for (l : layers) {
            n(c, l) = (n.dot(navg) > 0 ? -navg : navg);
        }
        a(c, l) = PlaneConstant(u(c, l), n(c, l), h);
    }
    return {n, a};
}
```

Normals n are estimated using the standard Youngs-centered scheme `Normal()` applied to stencil values assembled by `Stencil3()`, which selects values with given color (or zero if the requested color is not found) on the $3 \times 3 \times 3$ stencil. After all advection sweeps, `Recolor()` detects new connected components and recomputes the colors as described in *Connected-component labeling*.

The complete implementation of the multilayer VOF is given in `src/solver/vofm.ipp`.

5.1 Connected-component labeling

After each advection step, the colors need to be updated to detect new connected components. The following function initializes the color field with unique values, then iteratively joins the colors from adjacent cells by taking the minimal color until equilibration.

```
auto Recolor(u, q) {
    q_new = InitUnique(u, q);

    changed = true;
    while (changed) {
        changed = false;
        q_new = RecolorCorners(u, q, q_new);
        for (c : cells) {
            for (l : layers) {
                for (cn : stencil3(c)) {
                    ln = FindLayer(q, cn, q(c, l));
                    if (ln != kLayerNone) {
                        if (q_new(cn, ln) < q_new(c, l)) {
```

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```
        changed = true;
        q_new(c, l) = q_new(cn, ln);
    }
}
}
}
}
return q_new;
}
```

To reduce the number of iterations, function `RecolorCorners()` runs the same algorithm for corners from cubic subdomains. The colors propagate through the domain faster.

```
auto RecolorCorners(u, q, q_new) {
    // map: mapping from old color to new color
    for (c : corners of subdomains) {
        for (l : layers) {
            for (size_t d : {0, 1, 2}) {
                cn = AdjacentCell(c, d);
                ln = FindLayer(q, cm, q(c, l));
                q1 = q_new(c, l);
                q2 = q_new(cn, ln);
                map[max(q1, q2)] = min(q1, q2);
            }
        }
    }

    changed = true;
    while (changed) {
        changed = false;
        for (q1 in map) {
            if (map[q1] in map) {
                map[q1] = map[map[q1]];
                changed = true;
            }
        }
    }

    for (f : faces) {
        cm = AdjacentCell(f, 0);
        cp = AdjacentCell(f, 1);
        for (l : layers) {
            q_new(cm, l) = map[q(cm, l)];
            q_new(cp, l) = map[q(cp, l)];
        }
    }
    return q_new;
}
```

6 Embedded boundaries

The method of embedded boundaries allows one to solve equations in complex geometries on a Cartesian mesh. The surface of a solid body is represented by *cut cells*. A cut cell is obtained by cutting a regular cubic cell with a plane. Discretization of the equations with the finite volume method remains the same, except that the discrete conservation law now includes additional boundaries in cut cells.

The functionality related to embedded boundaries is provided in header `embed.h`.

```
#include <aphros/solver/embed.h>
```

A new type `FieldEmbed` transparently combines `FieldFace` and `FieldCell`. The cell-field stores the values on embedded boundaries. Given a mesh `m`, a combined field is initialized on the mesh similar to other fields with an optional default value:

```
FieldEmbed<Scal> fe(m, 0); // [f]ield [e]mbed
```

The field can be accessed both by cell- and face-indices. The following code traverses all internal cells and faces and assigns a value to the field:

```
for (IdxCell c : m.Cells()) {
    fe[c] = 1;
}
for (IdxFace f : m.Faces()) {
    fe[f] = 1;
}
```

A new class `Embed<M>` defines new iterators and geometric routines that take into account cut cells. The cells and faces are divided into three groups:

- regular cells (whole cells inside the domain),
- cut cells (cells crossed by the domain boundary),
- excluded cells (cells outside the domain).

The same classification applies to faces

- regular faces (whole faces inside the domain),
- cut faces (faces crossed by the domain boundary),
- excluded faces (cells outside the domain).

An instance of `Embed<M>`, commonly named as `eb`, is constructed from a mesh and needs to be initialized from a level-set function φ stored in a node-field:

```
void F(const FieldNode<Scal>& phi) {
    auto sem = m.GetSem();
    struct {
        std::unique_ptr<Embed<M>> eb_;
    } * ctx(sem);
    if (sem()) {
        eb_.reset(new Embed<M>(m));
    }
    if (sem.Nested()) {
        eb_->Init(phi);
    }
}
```

Regular cells are those for which $\varphi > 0$ in all adjacent nodes, excluded cells are those for which $\varphi < 0$ in all adjacent nodes, and other cells are cut cells. The `Embed<M>` class defines ranges `eb.Cells()` and `eb.Faces()` such that they include regular and cut cells but not excluded cells. Another range `eb.CFaces()` traverses only cut cells. The name `CFaces` comes from *Cell Faces*. Together, `eb.Faces()` and `eb.CFaces()` include all indices for which an embed-field can be defined. The following code assigns a value to the embed-field in cut cells, regular faces and cut faces:

```
for (IdxCell c : eb.CFaces()) {
    fe[c] = 1;
}
for (IdxFace f : eb.Faces()) {
    fe[f] = 1;
}
```

Class `Embed<M>` also defines geometric routines such as `eb.GetVolume()` and `eb.GetArea()`. The following code computes the total volume of the domain and the total area of all boundaries:

```
Scal vol = 0;
for (IdxCell c : eb.Cells()) {
    vol += eb.GetVolume(c);
}
Scal area = 0;
for (IdxFace f : eb.Faces()) {
    area += eb.GetArea(f);
}
for (IdxCell c : eb.CFaces()) {
    area += eb.GetArea(c);
}
```

The range of neighbor indices `eb.Nci()` is limited to non-excluded neighbor faces. The name `Nci` stands for *Neighbor Cell Index*. The following code sums up the values over all faces of one cut cell `c`:

```
IdxCell c;
Scal sum = fe[c];
for (size_t q : eb.Nci()) {
    IdxFace f = eb.GetFace(c, q);
    sum += fe[f];
}
```

The header defines numerical routines for interpolation and computation of gradients. Some of them require boundary conditions.

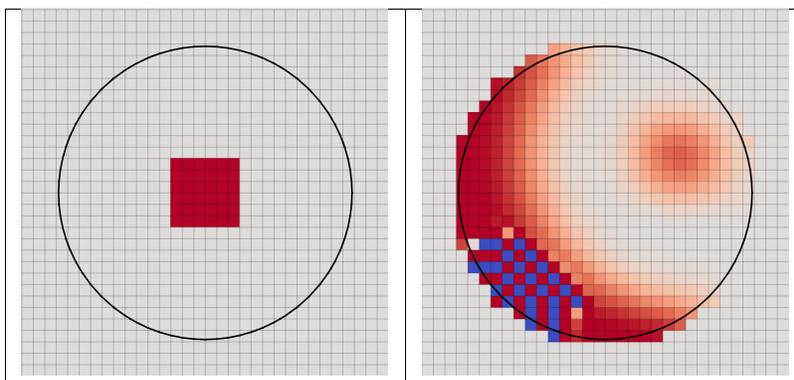
```
MapEmbedCond mec; // boundary conditions
FieldEmbed<Scal> feu(m);
FieldCell<Scal> fcu(m);
FieldCell<Scal> fci = eb.Interpolate(feu);
FieldEmbed<Scal> fei = eb.Interpolate(fcu, mec);
FieldCell<Vect> fcg = eb.Gradient(feu);
FieldEmbed<Scal> feg = eb.Gradient(fcu, mec);
```

6.1 Advection solver

The routines described above are sufficient to implement an advection solver.

```
// Advection solver.
// fcu: quantity to advect
// mebc: boundary conditions
// vel: advection velocity
// dt: time step
void Advection0(
    FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc,
    const FieldEmbed<Scal>& fev, Scal dt, const Embed<M>& eb) {
    const auto fcg =
        UEmbed<M>::GradientLinearFit(UEmbed<M>::Interpolate(fcu, mebc, eb), eb);
    const auto feu =
        UEmbed<M>::InterpolateUpwind(fcu, mebc, ConvSc::fou, fcg, fev, eb);
    // Compute flux.
    FieldEmbed<Scal> fevu(eb, 0);
    for (auto f : eb.Faces()) {
        fevu[f] = feu[f] * fev[f];
    }
    for (auto c : eb.CFaces()) {
        fevu[c] = feu[c] * fev[c];
    }
    // Advance in time.
    for (auto c : eb.Cells()) {
        Scal sum = fevu[c]; // sum of fluxes
        for (auto q : eb.Nci(c)) {
            sum += fevu[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
        }
        fcu[c] -= sum * dt / eb.GetVolume(c);
    }
}
```

Table 6.1: Results of advection solver `Advection0()`: initial (left) and final (right). Instabilities develop near the boundary.



See full example in [examples/103_embed_advection/main.cpp](#).

The previous implementation suffers from the problem of small cells. Stability requires that the change of the conserved quantity at one time step does not exceed the cell volume. Therefore, small cells lead to strong restrictions on the time step. One common remedy is redistribution of the conserved quantity to neighboring cells. Function `eb.RedistributeCutCells()` redistributes a conserved quantity from cut cells to their neighboring cells such that the integral of the quantity does not change. Using this function in the advection solver results in

```

// Advection solver with redistribution from cut cells
// and first order upwind scheme.
void Advection1(
    FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc,
    const FieldEmbed<Scal>& fev, Scal dt, const Embed<M>& eb) {
    const auto fcg =
        UEmbed<M>::GradientLinearFit(UEmbed<M>::Interpolate(fcu, mebc, eb), eb);
    const auto feu =
        UEmbed<M>::InterpolateUpwind(fcu, mebc, ConvSc::fou, fcg, fev, eb);
    // Compute flux.
    FieldEmbed<Scal> fevu(eb, 0);
    for (auto f : eb.Faces()) {
        fevu[f] = feu[f] * fev[f];
    }
    for (auto c : eb.CFaces()) {
        fevu[c] = feu[c] * fev[c];
    }
    // Compute the change at one time step.
    FieldCell<Scal> fct(eb, 0);
    for (auto c : eb.Cells()) {
        Scal sum = fevu[c];
        for (auto q : eb.Nci(c)) {
            sum += fevu[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
        }
        fct[c] = -sum * dt;
    }
    fct = UEmbed<M>::RedistributeCutCells(fct, eb);
    // Advance in time.
    for (auto c : eb.Cells()) {
        fcu[c] += fct[c] / eb.GetVolume(c);
    }
}

```

```

// Advection solver with redistribution from cut cells
// and second order upwind scheme.
void Advection2(
    FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc,
    const FieldEmbed<Scal>& fev, Scal dt, const Embed<M>& eb) {
    const auto fcg =
        UEmbed<M>::GradientLinearFit(UEmbed<M>::Interpolate(fcu, mebc, eb), eb);
    auto feu = UEmbed<M>::InterpolateUpwind(fcu, mebc, ConvSc::sou, fcg, fev, eb);
    // Compute flux.
    FieldEmbed<Scal> fevu(eb, 0);
    for (auto f : eb.Faces()) {
        fevu[f] = feu[f] * fev[f];
    }
    for (auto c : eb.CFaces()) {
        fevu[c] = feu[c] * fev[c];
    }
    // Compute the change at one time step.
    FieldCell<Scal> fct(eb, 0);
    for (auto c : eb.Cells()) {
        Scal sum = fevu[c];
        for (auto q : eb.Nci(c)) {
            sum += fevu[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
        }
        fct[c] = -sum * dt;
    }
}

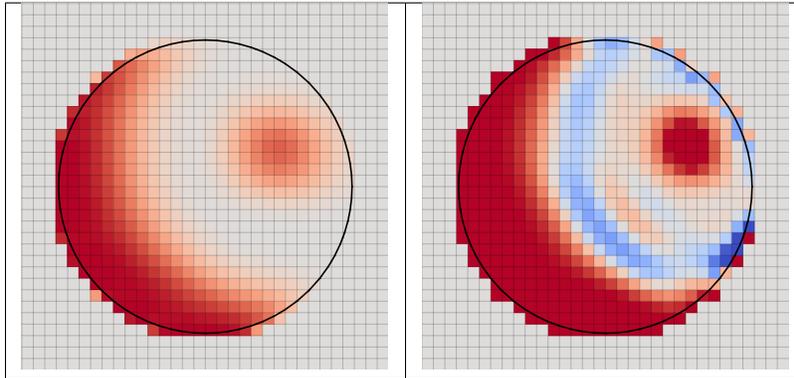
```

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```
}  
fct = UEmbed<M>::RedistributeCutCells(fct, eb);  
// Advance in time.  
for (auto c : eb.Cells()) {  
    fcu[c] += fct[c] / eb.GetVolume(c);  
}  
}
```

Table 6.2: Results of first order upwind scheme `Advection1()` (left) and second order upwind scheme `Advection2()` (right). Redistribution from cut cells stabilizes the method in both cases.



The fraction of redistributed quantities `eb.RedistributeCutCells()` does not depend on the velocity or the time step. While this makes a stable method, the unnecessary redistribution of values may reduce the accuracy. Another approach would be to use a local stability criterion depending on the velocity

$$\frac{v_f \Delta t}{S_f |\mathbf{x}_c - \mathbf{x}_f|} < \text{CFL}_0$$

6.2 Diffusion solver

The diffusion equation illustrates another problem of small cells which arises in computation of gradients. The diffusive fluxes are proportional to the normal gradient of the quantity. Approximations of normal gradients contain the distance between the face and cell centroids in the denominator.

$$\left(\frac{\delta u}{\delta n}\right) = \frac{u_c - u_f}{(\mathbf{x}_c - \mathbf{x}_f) \cdot \mathbf{n}_f}$$

The following function implements a diffusion solver using this approximation

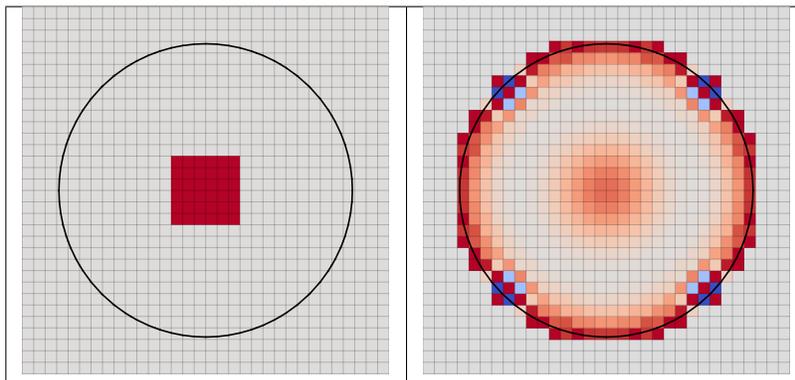
```
// Diffusion solver.  
// fcu: quantity to advect  
// mebc: boundary conditions  
// diff: diffusion coefficient  
// dt: time step  
void Diffusion0(  
    FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc, Scal diff, Scal dt,  
    const Embed<M>& eb) {  
    const auto feg = UEmbed<M>::Gradient(fcu, mebc, eb);  
    // Compute flux.  
    FieldEmbed<Scal> fed(eb, 0);
```

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```
for (auto f : eb.Faces()) {
    fed[f] = feg[f] * diff * eb.GetArea(f);
}
for (auto c : eb.CFaces()) {
    fed[c] = feg[c] * diff * eb.GetArea(c);
}
// Advance in time.
for (auto c : eb.Cells()) {
    Scal sum = fed[c]; // sum of fluxes
    for (auto q : eb.Nci(c)) {
        sum += fed[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
    }
    fcu[c] += sum * dt / eb.GetVolume(c);
}
}
```

Table 6.3: Results of diffusion solver `Diffusion0()`: initial (left) and final (right). Instabilities develop near the boundary.



See full example in `examples/104_embed_diffusion/main.cpp`.

```
// Diffusion solver with redistribution to neighbor cells.
void Diffusion1(
    FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc, Scal diff, Scal dt,
    const Embed<M>& eb) {
    const auto feg = UEmbed<M>::Gradient(fcu, mebc, eb);
    // Compute flux.
    FieldEmbed<Scal> fed(eb, 0);
    for (auto f : eb.Faces()) {
        fed[f] = feg[f] * diff * eb.GetArea(f);
    }
    for (auto c : eb.CFaces()) {
        fed[c] = feg[c] * diff * eb.GetArea(c);
    }
    // Compute the change at one time step.
    FieldCell<Scal> fct(eb, 0);
    for (auto c : eb.Cells()) {
        Scal sum = fed[c];
        for (auto q : eb.Nci(c)) {
            sum += fed[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
        }
        fct[c] = sum * dt;
    }
}
```

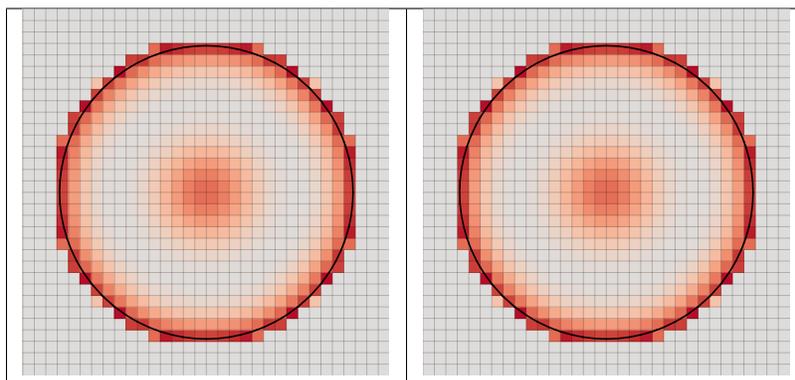
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```
}
fct = UEmbed<M>::RedistributeCutCells(fct, eb);
// Advance in time.
for (auto c : eb.Cells()) {
    fcu[c] += fct[c] / eb.GetVolume(c);
}
}
```

```
// Diffusion solver with redistribution to neighbor cells
// and LoopFaces() to avoid code duplicatoin.
void Diffusion2(
    FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc, Scal diff, Scal dt,
    const Embed<M>& eb) {
    const auto feg = UEmbed<M>::Gradient(fcu, mebc, eb);
    // Compute flux.
    FieldEmbed<Scal> fed(eb, 0);
    eb.LoopFaces([&](auto cf) { // lambda-function applied to faces and
                               // embedded faces
        fed[cf] = feg[cf] * diff * eb.GetArea(cf);
    });
    // Compute the change at one time step.
    FieldCell<Scal> fct(eb, 0);
    for (auto c : eb.Cells()) {
        Scal sum = fed[c];
        for (auto q : eb.Nci(c)) {
            sum += fed[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
        }
        fct[c] = sum * dt;
    }
    fct = UEmbed<M>::RedistributeCutCells(fct, eb);
    // Advance in time.
    for (auto c : eb.Cells()) {
        fcu[c] += fct[c] / eb.GetVolume(c);
    }
}
```

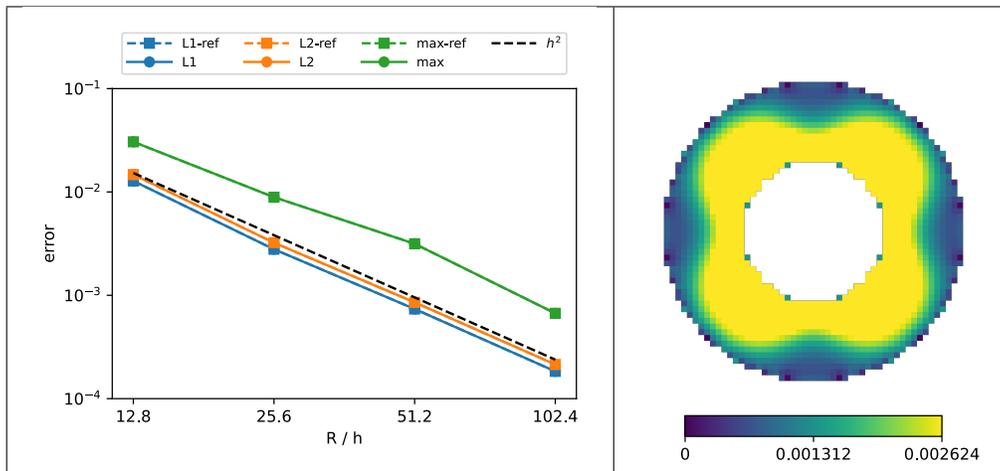
Table 6.4: Results of diffusion solver Diffusion1() (left) using linear fit to cell centers to compute the gradient which eliminates the instabilities. Solver Diffusion2() (right) produces the same results and illustrates the usage of ExecFaces() to execute the same lambda-function on indices of two types



6.3 Taylor-Couette flow

See full example in [examples/201_taylor_couette](#).

Table 6.5: Error norms with grid refinement (left) and error field at $R/h = 25.6$ (right).

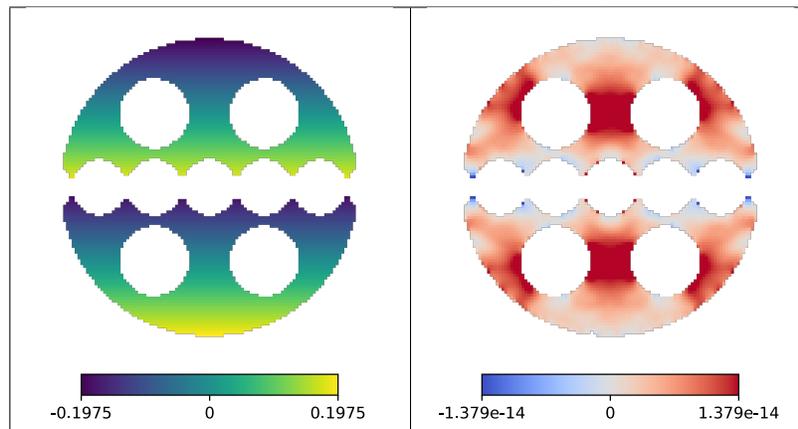


6.4 Hydrostatic

Single-phase

See full example in [examples/203_hydrostatic](#).

Table 6.6: Pressure (left) and velocity (right).



Multiphase

See full example in [examples/203_hydrostatic](#).

Table 6.7: Initial density (top left), final density (top right), pressure (bottom left) and velocity (bottom right).

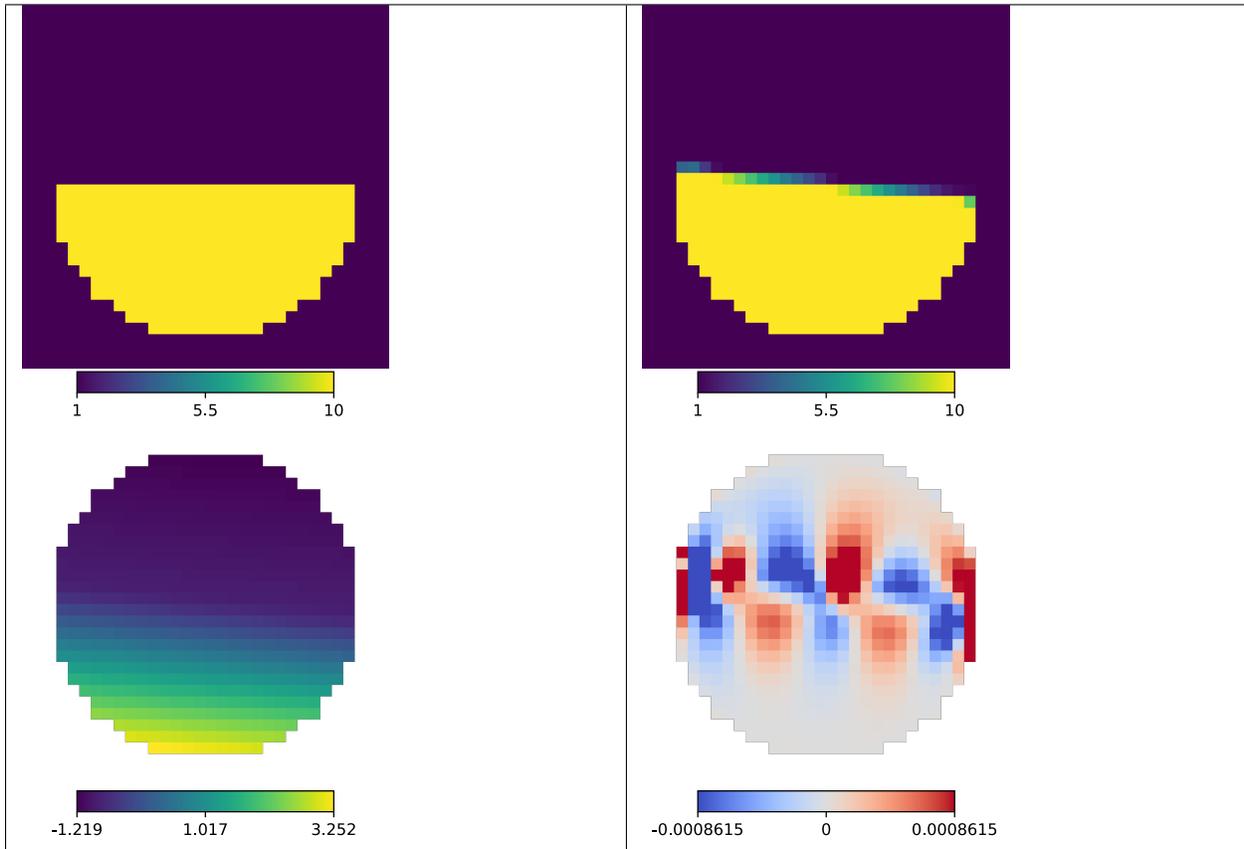
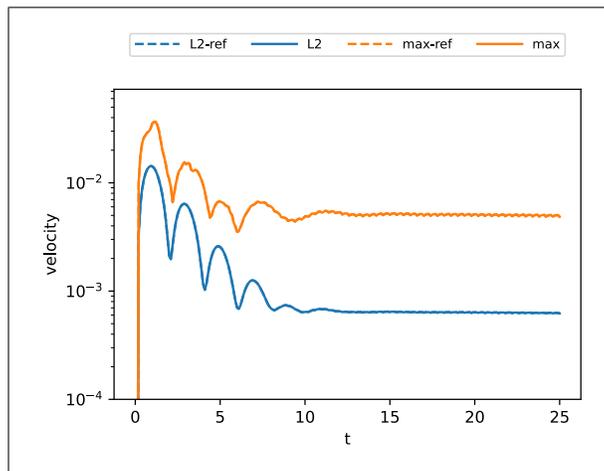


Table 6.8: Evolution of velocity norms.



7 Geometric primitives

Header `func/primlist.h` provides routines to define level-set functions for a list of geometric primitives such as spheres and boxes. A primitive is described by

```
struct Primitive {
    using Vect = Vect_;
    using Scal = typename Vect::Scal;
    static constexpr size_t dim = Vect::dim;

    Primitive(std::string name_)
        : name(name_), inter([](const Rect<Vect>&) -> bool { return true; }) {}
    Primitive() : Primitive("") {}
    friend std::ostream& operator<<(std::ostream& o, const Primitive<Vect>& p) {
        o << "name=" << p.name << " ";
        o << " mod=" << (p.mod_minus ? "-" : "") << (p.mod_and ? "&" : "") << " ";
        return o;
    }

    std::string name;
    bool mod_minus = false;
    bool mod_and = false;
    std::function<Scal(const Vect&)> ls; // level-set
    std::function<bool(const Rect<Vect>&)> inter; // true if intersects rectangle
    std::function<Vect(const Vect&)> velocity; // velocity

    Vect c; // center XXX adhoc for GetSphereOverlap
    Vect r; // radius XXX adhoc for GetSphereOverlap
};
```

Function `GetPrimitives()` parses a stream with a list of primitives.

```
// Parses a list of primitives in stream buf.
// edim: effective dimension, 2 or 3 (ignores z-component if edim=2)
static std::vector<Primitive> GetPrimitives(std::istream& buf, size_t edim)
```

Available primitives and their parameters:

sphere Ellipsoid with principal axes aligned with the coordinate axes. Parameters: `cx cy cz` (center), `rx ry rz` (half-size);

box Rectangular box with sides aligned with the coordinate planes. Parameters: `cx cy cz` (center), `rx ry rz` (half-size);

ring Torus. Parameters: `cx cy cz` (center), `nx ny nz` (normal), `r` (radius), `th` (thickness);

smooth_step Smooth step Almgren *et al.* [2]. Parameters: `cx cy cz` (center), `nx ny nz` (normal), `tx ty tz` (tangent), `ln` (size along normal), `lt` (size along tangent);

cylinder Right circular cylinder. Parameters: `cx cy cz` (center), `nx ny nz` (normal), `r` (radius), `n0 n1` (range along normal relative to center);

polygon Cylinder bounded by parallel planes with the plane section specified as a sequence of non-intersecting polygons. Parameters: `ox oy oz` (origin), `nx ny nz` (normal), `ux uy uz` (direction of 2D x-axis), `n0 n1` (range along normal relative to origin), `scale` (factor applied to 2D vertices), `x y . . .` (2D vertices of all polygons, first and last vertices of each polygon must coincide);

ruled Ruled surface bounded by parallel planes with two plane sections on the opposite sides specified as two sequences of non-intersecting polygons. Parameters: `ox oy oz` (origin), `nx ny nz` (normal), `ux uy uz`

(direction of 2D x-axis), n_0 n_1 (range along normal relative to origin, sides 0 and 1), $scale_0$ $scale_1$ (factors applied to 2D vertices on sides 0 and 1), x y ... (2D vertices of all polygons on side 0, first and last vertices of each polygon must coincide), x y ... (same but on side 1).

Each primitive defines a level-set function which is positive inside the body. By default, the resulting level-set function is composed from the list of primitives using the union operation (taking the maximum value). To change the default operation, modifiers can be added before the name of the primitive:

- -: minus, multiply level-set by -1;
- &: intersection, take the minimum with the current level-set.

Example of a list of primitives

```
# cx cy cz  rx ry rz
box 0.7 0.3 0.4  0.25 0.2 0.15

&cylinder 0.55 0.25 0.5  0 0 1  0.22  -1 1
&-cylinder 0.7 0.3 0.4  1 0.5 0  0.07  -1 1

# cx cy cz  rx ry rz
sphere 0.3 0.3 0.7  0.25 0.2 0.15

&-box 0.45 0.3 0.7  0.1 0.2 0.03

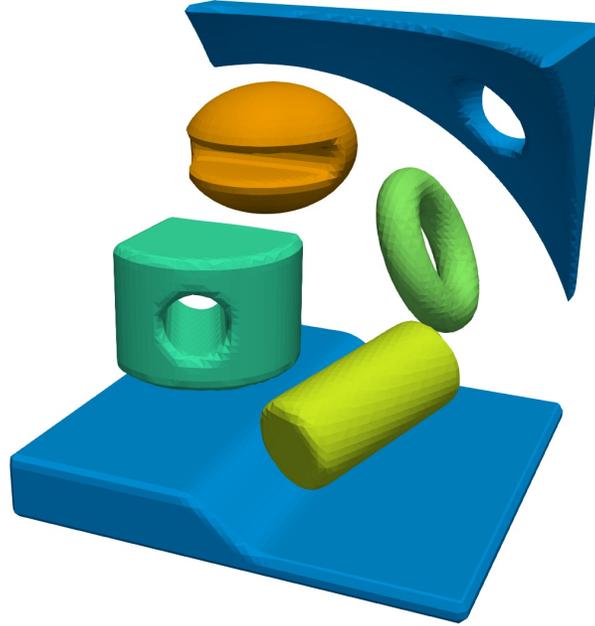
# cx cy cz nx  ny nz r th
ring 0.3 0.7 0.5  0 1 0.5  0.15  0.05

# cx cy cz  nx ny nz  tx ty tz  ln lt
smooth_step 0.5 0.5 0.1  0 0 1  0 1 0  0.05  0.1

# cx cy cz  tx ty tz  r  t0 t1
cylinder 0.75 0.7 0.3  -2 1 0.5  0.1  -0.2 0.2

-sphere 1 0.2 0  1.3
&-cylinder 0.1 0.8 0.8  -2 1 0.5  0.1  -0.2 0.2
```

(see setup in [examples/200_primlist](#))



Parameter `list_ls` in the configuration defines the method of computing the volume fraction field from the level-set functions

set int list_ls 0 step-wise approximation (1 if level-set is positive, 0 otherwise);

set int list_ls 1 linear approximation with normal and plane constant computed from the level-set at the cell center, does not support modifiers;

set int list_ls 2 using the `overlap` library to compute the exact volume fraction cut by an ellipsoid (only valid for primitive `sphere`);

set int list_ls 3 linear approximation with normal and plane constant computed from the level-set on mesh nodes, supports modifiers.

8 Boundary conditions

Header `func/init_u.h` provides routines to describe boundary conditions based on primitives. The list of boundary conditions is a list of code blocks with primitives.

8.1 Code blocks

A code block is described by

```
struct CodeBlock {
    std::string name;
    std::string content;
};
```

and has the following format

```
NAME {
    CONTENT
}
```

where NAME does not contain { or } and CONTENT may contain only matching { . . . }.

Examples of code blocks

```
name {
  content
}

name { content }

name with spaces {
  content { inside {inside} braces }
}
```

The following function extracts a list of blocks from a stream

```
// Parses a stream and returns a list of code blocks.
std::vector<CodeBlock> ParseCodeBlocks(std::istream& f)
```

Leading and trailing whitespaces are stripped.

8.2 Groups of primitives

Boundary conditions are selected inside groups of primitives organized as code blocks. The name of the block is the boundary condition to set and the content is a list of primitives describing a single level set function. Affected are cut cells and faces on the domain boundary.

```
wall 0 0 0 {
  box 0 0 0 10
}
wall 1 0 0 {
  sphere 0.7 0.5 0.5 0.2
}
slipwall {
  sphere 0.3 0.5 0.5 0.2
}
inlet 1 0 0 {
  sphere 0.5 0.7 0.5 0.2
}
symm {
  sphere 0.5 0.5 0.7 0.2
  sphere 0.5 0.5 0.3 0.2
}
```

The following function parses a file and returns a MapEmbed object containing face and cut-cell conditions.

```
MapEmbed<size_t>, MapEmbed<size_t>, std::vector<std::string>>
ParseGroups(
  std::istream& fin, const MEB& eb, const FieldCell<bool>& fc_innmask)
```

9 Output

Simulations produce output of various types:

- statistics (stdout)
- fields (HDF5, plain or XML VTK)
- PLIC polygons (polydata legacy VTK)
- marching cubes triangles (polydata legacy VTK)
- boundary conditions (polydata legacy VTK)

Boundary conditions are written to `bc.vtk` if enabled by `set int dumpbc 1`. It contains cell fields `block` (block id), `cond` (conditions for advection) and `condfluid` (conditions for fluid, see *Fluid boundary conditions*).

The output is implemented in function

```
void DumpBcPoly(  
    const std::string filename, const MapEmbed<size_t>& me_group,  
    const MapEmbed<typename MEB::Scal>& me_contang, const MEB& meb,  
    typename MEB::M& m)
```

10 Tools

10.1 AWK for CSV files

Synopsis

```
ap.cawk [-v var=value] ['prog'] [CSV ..]
```

Description

Examples

```
$ cat example.csv  
x,y  
1,10  
2,20  
$ ap.cawk '{print $x + $y}' example.csv  
11  
22
```

```
$ ap.cawk 'NR == 2 {print HEADER} {print $x + $y}' q  
x,y  
11  
22  
33
```

Source

10.2 Format

Synopsis

`ap.format [-y]`

runs clang-format for all C/C++ files found recursively from current directory.

`-y` Force 'yes' for all questions

Configuration

The configuration is based on Google code style with modifications.

`.clang-format`

Source

`deploy/scripts/format`

10.3 Histogram

Synopsis

`ap.hist [-density|-cumulative] [-bins BINS] [-range L R]`

print histogram of STDIN as columns [center,density,left,right]

Examples

```
seq 10 | ap.hist --density
seq 10 | ap.hist --cumulative
```

Source

`deploy/scripts/hist`

11 Library

11.1 VOF advection

Synopsis

Volume-of-fluid advection solver with PLIC reconstruction.

Parameters

```
struct VofPar {
    using Scal = typename M::Scal;
    using Vect = typename M::Vect;

    size_t dim = 3; // dimension (dim=2 assumes zero velocity in z)
    Scal clipth = 1e-10; // vf clipping threshold
    Scal filterth = 0; // orphan filtering threshold
    bool recolor = true; // run connected component labeling on every step
    bool recolor_unionfind = true; // use union-find algorithm
    bool recolor_reduce = true; // reduce set of colors to integers
    bool recolor_grid = true; // use grid heuristic
    Scal clfixed = -1; // if >= 0, value for color at point clfixed_x
    Vect clfixed_x = Vect(1e10);
    bool cloverride = false; // XXX adhoc if clear1<1, override color with 0
    bool sharpen = false;
    Scal sharpen_cfl = 0.5;
    size_t layers = 4;
    Scal avgnorm0 = 1; // original normal with sum(u)<avgnorm0
    Scal avgnorm1 = 1; // overridden normal with sum(u)>=acgnorm1
    Scal coalth = 1e10;
    int verb = 0;
    bool bcc_reflectpoly = true; // reflection for DumpPolyMarch
    Scal dumppolymarch_fill = -1; // fill cells outside
    bool vtkbin = true;
    bool vtkmerge = true;
    bool vtkpoly = true; // dump vtk polygins instead of lines
    Scal vtkiso = 0.5;
    enum class Scheme { plain, aulisa, weymouth };
    Scheme scheme = Scheme::weymouth;
    // Enables extrapolation to halo or cut cells,
    // required for the contact angle model.
    // Extrapolate volume fraction to excluded cells before computing normals
    // Extrapolate volume fraction, plane constant and normals to cut cells
    // after the advection step.
    // If embedded boundaries are enabled, supports only periodic condttions.
    bool extrapolate_boundaries = false;
    Labeling<M>* labeling = nullptr; // Pointer to implementation of
    // connected component labeling.
    // Defaults to Recolor().
};
```

Source

```
src/solver/vof.h
src/solver/vof.cpp
src/solver/vof.ipp
```

Example

examples/100_advection/main.cpp

```
// Created by Petr Karnakov on 24.12.2019
// Copyright 2019 ETH Zurich

#undef NDEBUG
#include <cassert>
#include <iostream>
#include <memory>
#include <string>

#include <distr/distrbasic.h>
#include <solver/vof.h>

using M = MeshCartesian<double, 3>;
using Scal = typename M::Scal;
using Vect = typename M::Vect;

void Run(M& m, Vars&) {
    auto sem = m.GetSem();

    struct {
        std::unique_ptr<Vof<M>> as; // advection solver
        FieldCell<Scal> fc_src; // volume source
        FieldEmbed<Scal> fe_flux; // volume flux
        MapEmbed<BCondAdvection<Scal>> mf_cond; // face conditions
    } * ctx(sem);

    auto& as = ctx->as;
    const Scal tmax = 1.;
    const Vect vel(0.5, 0.3, 0.1);
    const Scal cfl = 0.5;

    if (sem("init")) {
        auto& fc_src = ctx->fc_src;
        auto& fe_flux = ctx->fe_flux;
        auto& mf_cond = ctx->mf_cond;

        fc_src.Reinit(m, 0);
        fe_flux.Reinit(m, 0);
        for (auto f : m.Faces()) {
            fe_flux[f] = vel.dot(m.GetSurface(f));
        }
        FieldCell<Scal> fccl(m, 0); // initial color
        FieldCell<Scal> fcu(m, 0); // initial volume fraction
        for (auto c : m.Cells()) {
            fcu[c] = (m.GetCenter(c).dist(Vect(0.5, 0.5, 0.5)) < 0.2);
        }
        const Scal dt = cfl * m.GetCellSize()[0] / vel.norm();
        typename Vof<M>::Par p;
        as.reset(
            new Vof<M>(m, m, fcu, fccl, mf_cond, &fe_flux, &fc_src, 0., dt, p));
    }
    sem.LoopBegin();
    if (sem.Nested("start")) {
        as->StartStep();
    }
}
```

(continues on next page)

```

}
if (sem.Nested("iter")) {
    as->MakeIteration();
}
if (sem.Nested("finish")) {
    as->FinishStep();
}
if (sem("checkloop")) {
    if (as->GetTime() >= tmax) {
        sem.LoopBreak();
    }
}
if (sem("dump")) {
    m.Dump(&as->GetField(), "u");
}
if (sem()) {
}
sem.LoopEnd();
}

int main(int argc, const char** argv) {
    std::string conf = R"EOF(
set int bx 1
set int by 1
set int bz 1

set int bsx 16
set int bsy 16
set int bsz 16

set int px 1
set int py 1
set int pz 1
)EOF";

    MpiWrapper mpi(&argc, &argv);
    return RunMpiBasicString<M>(mpi, Run, conf);
}

```

12 Log

12.1 Surface tension as gradient

2018-08-30 22:08:47

Goal: zero integral of force

What: surface tension as $\nabla(\kappa\alpha)$ on faces, curvature in cells copied from neighbour faces if nan.

Result: instability for test of single drop equilibrium,

Data: doc/sphinx/src/log/log01_grad_ka

- doc/sphinx/src/log/log01_grad_ka/grad_ka.mp4: surface tension as $\nabla(\kappa * \alpha)$
- doc/sphinx/src/log/log01_grad_ka/k_grad_a.mp4: surface tension as $\kappa \nabla \alpha$

- [doc/sphinx/src/log/log01_grad_ka/k_grad_a_kmean.mp4](#): mean curvature on face if both cells contain interface

12.2 Particle normal displacement

2018-09-02 09:41:49

Goal: reduce spurious flow and deformation for single drop equilibrium

What: particle strings without normal displacement, position of central particle fixed at the interface line center

Result: deformation of the interface greatly reduced, probably due to stronger coupling or penalization of deformed interfaces

Data: [doc/sphinx/src/log/log02_dn](#)

- [doc/sphinx/src/log/log02_dn/dn0.mp4](#): without normal displacement
- [doc/sphinx/src/log/log02_dn/dn1.mp4](#): with normal displacement

12.3 march=native

2018-09-09 11:59:47

Goal: use automatic vectorization and specific optimizations

What: add `-march=native` to `CMAKE_C_FLAGS` and `CMAKE_CXX_FLAGS`

Result: slight improvement of performance (3.60 vs 3.76 s for `confdiff:01:assemble`) with 64 cores on Euler

Data: [doc/sphinx/src/log/log03_native](#):

- `out_std`: standard flags
- `out_native`: `-march=native`

12.4 max_iter

2018-09-12 14:03:27

Goal: choose optimal number of iterations `max_iter`

What: Taylor-Green with bubbles (`sim06`) with `max_iter=1,2,3,4,5` and `convsc=cd,quick`.

Result

- qualitatively different trajectories for `max_iter=1,2`;
- convergence at `max_iter=4`
- no major difference between `cd` and `quick`,
- no difference between `simpler=0` and `1`

Data: [doc/sphinx/src/log/log04_maxit](#)

- `kedr.pdf`: kinetic energy dissipation rate
- `traj.pdf`: x-component of trajectory of bubble 2

12.5 Number of particles and strings

Goal: check the influence of the `part_np` and `part_ns` in curvature estimator

What: Free-field coalescence of bubbles based on `sim04_univel`

Result

- slight differences in shapes comparing `np=5, 0` and `ns=2, 3`

Data: [doc/sphinx/src/log/log05_coalnp](#)

- `gen1_ns3_np5`: configuration
- `nx064_ns?_np?.png`: shapes at `t=0.466` with `nx=64`
- `nx128_ns2_np9.png`: shapes at `t=0.466` with `nx=128`

12.6 Number of iterations for coalescence

Goal: check the influence of the `min_iter` and `tol` on bubble coalescence

What: Free-field coalescence of bubbles based on `sim04_univel/case/partstrcoal`

Result

- negligible difference in trajectories between default and `min_iter=10`

Data: [doc/sphinx/src/log/log06_coaliter](#)

- `nx*iter*`: configuration, data, movie
- `a.gnu`: gnuplot script

12.7 Relaxation parameters

2019-03-21 22:48:56

Goal: check the influence of `vrelax` and `prelax` on bubble coalescence

What: Near-wall coalescence of bubbles with `vrelax=0.8, prelax=0.8` and `vrelax=0.9, prelax=1`

Result

- spurious oscillations in the pressure field (`wforce`) with `vrelax=0.9` after the bubble detachment
- no effect on x- and y-trajectories, slower rising in z after detachment
- changed default parameters for `sim04` to `prelax=0.8, vrelax=0.8` and `min_iter=4`

Data: [doc/sphinx/src/log/log07_vrelax](#)

- `gen1`: generator of parameters for `sim04/gen`
- `wforce`: force acting on `z=0` and `z=1`
- `out, stat.dat`: log and statistics

12.8 Reduced usage of GetCenter

2019-04-27 01:19:03

Goal: Performance improvement.

What: Reduced usage of `GetCenter` and `GetVectToCell`. Test of the Taylor-Green vortex with bubbles.

Result: Speedup of 15%.

Data [doc/sphinx/src/log/log08_getcenter](#)

- `tg`: setup
- `tg0_*`: timings before
- `tg1_*`: timings after

12.9 Debug linear solver with ConvertLsCompact

2019-08-15 10:04:39

Goal: Fix `sim12_ringgauss` after reimplementing `simple.ipp` with `ConvertLsCompact` in 48fa3cf0. Iterations for pressure correction diverged.

What: Bisection between 1ffd55c5 from Jan 12 2019 and 9cb90989 from Aug 14 2019. Complication from another bug in `InitVort()` which attempted to use uninitialized `fs_` in `hydro.h` (fixed by patch).

Result: Found the problem by printing the coefficients of the linear system before and after `ConvertLs()` or `ConvertLsCompact()`. The problem appeared from changing the order of stencil cells. In `sim12`, the symmetric linear solver is called twice: for initialization of vorticity and for pressure correction. Then `Hypre` is apparently initialized only once and that instance is used for both cases which leads to the wrong order of coefficients.

Data: [doc/sphinx/src/log/log09_debug_linear](#)

- `patch`: fix for `InitVort()`
- `r`: tool to apply patch and rebuild
- `simple_{bad,good}.ipp`: two versions of `simple.ipp`
- `min`: minimal simulation setup

12.10 Registered modules in Ubuntu

2020-06-03 11:34:54

Ubuntu has `--as-needed` by default (seen from `gcc -dumpspecs`) which makes the linker ignore unused libraries and, in particular, the implementations of modules (e.g. `init_contang.so`).

12.11 VTK merge, comparison of floats with tolerance

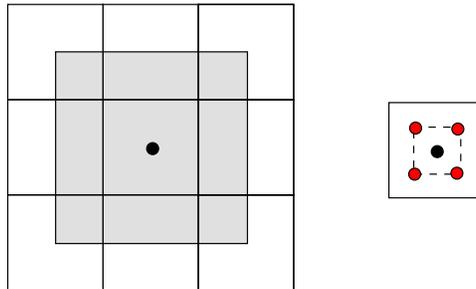
2020-06-13 21:56:35

`ConvertMerge` in `dump/vtk.h` mapped each `Vect` to a hash and used the hash to merge closely located points together (up to tolerance `tol`). This effectively split the space of `Vect` to partitions. However, if two points are located close to the boundary between two partitions, they can be arbitrarily close but have different hash values.

The solution was to check compare against the hash of neighboring points (from vertices of a cube) when looking for an existing hash.

Minimal example that gave vertices of rank 1: [doc/sphinx/src/log/log10_vtkmerge](#).

The opposite problem: hash collisions of distant points. Example is in `log10_vtkmerge/hash_collision`. To fix, changed the map from `hash->index` to `Vect->index` (ensures exact comparison of points) and introduced `canonical(x)` to get a single point from the cell of size `tol`.



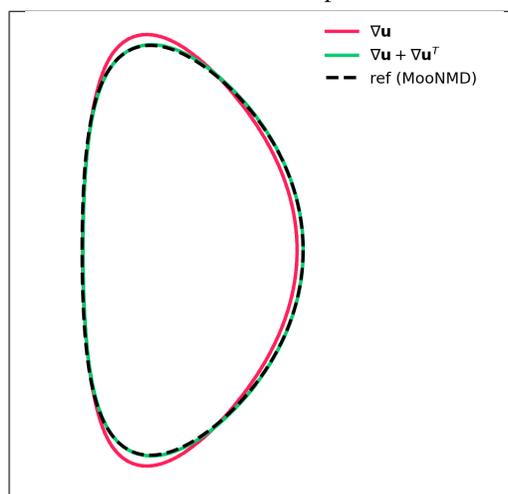
12.12 Explicit part of viscous stress

2021-06-11 15:32:27

The viscous stress tensor has the form $\mu(\nabla\mathbf{u} + \nabla\mathbf{u}^T)$. Parameter `int explviscous` controls whether the second term is included in the discretization. Setting `explviscous=0` changes the approximated tensor to $\mu\nabla\mathbf{u}$. This omitted term $\mu\nabla\mathbf{u}^T$ is significant if the dynamic viscosity is non-uniform.

The following test case of a rising bubble (based on <http://basilisk.fr/src/test/rising.c>) shows a small difference. See full example in [examples/208_rising](#).

Table 12.1: Bubble shapes at $t = 3$



13 Contributing

13.1 Style guide

Use [Google C++ Style Guide](#).

Loop indices:

- `i` - generic
- `c` - `IdxCell`
- `f` - `IdxFace`
- `w` - `MIdx`
- `d` - direction
- `d` - index `0 .. dim-1`

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